# **Ultrasonic Determination of Elastic Properties**

#### Procedure

- Time of flight measurements together with a known material thickness allow the determination of the sound velocity of longitudinal (c<sub>L</sub>) and transverse (c<sub>T</sub>) waves.
- The elastic modulus E and the shear modulus G can be determined out of  $c_L$  und  $c_T$  knowing the density (p):

$$E = 4 \rho c_T^2 \frac{3/4 - (c_T/c_L)^2}{1 - (c_T/c_L)^2} \qquad G = \rho c_T^2$$

## **Example: Contact Technique**

- Determination of c<sub>L</sub> with a longitudinal probe
- Determination of  $c_T$  with a transverse probe

## **Example: Immersion Technique**

- Water transmits only longitudinal waves
- Determination of c<sub>L</sub> out of the time of flight between the entrance echo and the backwall echo (perpendicular insonification).
- There are certain experimental conditions (dependent on probe and material) where partial wave mode conversions longitudinal ↔ transverse occur. Out of the corresponding LT echo one can determine c<sub>T</sub>.

# Example: Transmission with Air-Coupling

• Out of the temporal difference Δt between transmission signals with and without the sample one can determine it's longitudinal sound velocity c<sub>L</sub>:

$$\boldsymbol{c}_{L} = \frac{1}{1/\boldsymbol{c}_{Air} - \Delta t/d}$$

- d = Thickness of the sample
- c<sub>Air</sub> = Sound velocity of air (temperature dependent!)

#### **Example: Surface Waves**

- Oblique insonification in immersion: Creation of surface waves in sample
- Reception of leaky waves by oblique probe
- Time of flight measurements at different receiver positions allow the determination of the propagation velocity of the surface wave.
- Reference: J. Neuenschwander, T. Schmidt, T. Lüthi, and M. Romer, Leaky Rayleigh wave investigation on mortar samples, Ultrasonics, 45 (2006) 50-55.